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# Sulfur Deactivation of NO<sub>x</sub> Storage Catalysts: A Multiscale Modeling Approach

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**Résumé — Empoisonnement des matériaux de stockage des NO<sub>x</sub> par le soufre : approche multi-échelles** — Les pièges à NO<sub>x</sub> représentent une technologie prometteuse pour la réduction des émissions d'oxydes d'azote issus des moteurs opérant en mélange pauvre. Leur utilisation est limitée par la présence de composés soufrés dans les gaz d'échappement. Le soufre contenu dans le carburant et le lubrifiant est oxydé lors de la combustion en SO<sub>2</sub> et SO<sub>3</sub>. Ces oxydes de soufre présentent une forte affinité pour le matériau de stockage du piège, la formation de sulfate étant favorisée thermodynamiquement. Cette formation contribue au blocage des sites d'adsorption des NO<sub>x</sub> et influence l'opération de l'organe de post-traitement. La modélisation moléculaire représente un outil précieux pour prédire le comportement et les performances du système catalytique. Notre étude présente une méthodologie d'exploitation des calculs *ab initio* pour la formulation de modèles cinétiques développés dans la librairie de post-traitement véhicule *IFP Exhaust*. Nous illustrons notre approche par le cas de l'adsorption de SO<sub>3</sub> sur un matériau modèle, BaO. Afin d'obtenir une description fidèle du matériau de stockage réel, l'adsorption de SO<sub>3</sub> est décrite sur plusieurs sites : terrasses, marches, crans et le site massique. Des analyses de sensibilité et de vitesses de réactions permettent d'obtenir une compréhension plus approfondie des phénomènes d'empoisonnement mis en jeu.

**Abstract — Sulfur Deactivation of NO<sub>x</sub> Storage Catalysts: A Multiscale Modeling Approach** — *Lean NO<sub>x</sub> Trap (LNT) catalysts, a promising solution for reducing the noxious nitrogen oxide emissions from the lean burn and Diesel engines, are technologically limited by the presence of sulfur in the exhaust gas stream. Sulfur stemming from both fuels and lubricating oils is oxidized during the combustion event and mainly exists as SO<sub>x</sub> (SO<sub>2</sub> and SO<sub>3</sub>) in the exhaust. Sulfur oxides interact strongly with the NO<sub>x</sub> trapping material of a LNT to form thermodynamically favored sulfate species, consequently leading to the blockage of NO<sub>x</sub> sorption sites and altering the catalyst operation. Molecular and kinetic modeling represent a valuable tool for predicting system behavior and evaluating catalytic performances. The present paper demonstrates how fundamental ab initio calculations can be used as a valuable source for designing kinetic models developed in the IFP Exhaust library, intended for vehicle simulations. The concrete example we chose to illustrate our*

*approach was SO<sub>3</sub> adsorption on the model NO<sub>x</sub> storage material, BaO. SO<sub>3</sub> adsorption was described for various sites (terraces, surface steps and kinks and bulk) for a closer description of a real storage material. Additional rate and sensitivity analyses provided a deeper understanding of the poisoning phenomena.*

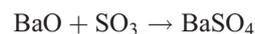
## INTRODUCTION

Lean-burn engines are gaining the European market share. Their attractiveness is mainly linked to low consumption and low CO<sub>2</sub> emission, but also to advantageous de-tax systems existing in the EU. However, environmental concerns for pollutant emissions still remain the main drawback of lean-burning solutions. Since they operate in excess of oxygen, a removal of the unburned CO and hydrocarbons is easily achieved with a standard diesel oxidation catalyst, whereas NO<sub>x</sub> abatement requires using advanced exhaust gas after-treatment techniques.

One of the few technologies available on the market and capable of meeting the stringent emission legislations are the Lean NO<sub>x</sub> Trap (LNT) catalysts [1-3]. LNT operation is based on successive rich/lean cycles. During lean phases, NO oxidation to NO<sub>2</sub> over precious metal sites (typically Pt, Rh, and Pd) takes place. NO<sub>2</sub>, intrinsically more acidic than NO, then migrates toward the basic storage material where, it is converted and stored as nitrate. To regenerate the storage capacity of the trap, engine combustion is briefly switched to fuel-rich conditions, producing CO, H<sub>2</sub>, and unburned hydrocarbons that reduce the stored nitrates to N<sub>2</sub>. Among the storage materials proposed, barium oxide is widely accepted as the most prominent candidate for commercial vehicle de-NO<sub>x</sub> applications. Initially intended for storage of NO<sub>x</sub> as nitrates, its storage capacity is significantly altered in the presence of sulfur due to poisoning phenomena. SO<sub>x</sub> (SO<sub>2</sub> + SO<sub>3</sub>) are systematically generated as by-products of the combustion of organic sulfur compounds, species naturally occurring in fossil fuels. Sulfur oxides are thus inevitably present in the exhaust stream and the sulfation of BaO remains the main drawback for a large-scale implementation of LNT technologies.

Numerous experimental studies witness a greater thermodynamic stability of BaSO<sub>4</sub> in comparison to Ba(NO<sub>3</sub>)<sub>2</sub> that leads to a preferential formation of sulfates and alters the NO<sub>x</sub> storage capacity [4, 5]. Engine test bench essays confirm that commercial NO<sub>x</sub> adsorbents are extremely sulfur-sensitive and that even sophisticated ultra-low-sulfur fuels containing 10 ppm S poison the NO<sub>x</sub> storage function [6]. Exposure to SO<sub>2</sub> in the presence of O<sub>2</sub> leads to a disappearing of the carbonate IR bands on a model Pt/Ba/Al<sub>2</sub>O<sub>3</sub> catalyst and to their

progressive replacement by distinctive surface and bulk sulfate bands [7]. *In situ* infrared studies by Breen *et al.* [8] showed that barium carbonate can be replaced by barium sulfate by reaction with low concentrations of SO<sub>2</sub> in the presence of large quantities of CO<sub>2</sub> at temperatures up to 700°C. Chronologically, surface sulfates are the first to appear, followed by bulk BaSO<sub>4</sub> and bulk Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>. Furthermore, the NO<sub>x</sub> storage capacity decrease is found to be proportional to the amount of SO<sub>2</sub> to which the BaO-based storage material has been exposed [9]. It is commonly accepted that SO<sub>2</sub> undergoes oxidation to SO<sub>3</sub> over precious metal sites. Experiments over a Pt/Ba/Al<sub>2</sub>O<sub>3</sub> catalyst confirm that SO<sub>2</sub> + O<sub>2</sub> exposure results in the formation of SO<sub>3</sub> that is being trapped as sulfate according to the proposed reaction scheme [10].



SO<sub>3</sub> gradually accumulated on barium sites forms BaSO<sub>4</sub>, which prevents NO<sub>x</sub> storage to take place [9, 11]. Thus, understanding the way sulfur poisoning occurs on BaO through interactions with SO<sub>3</sub> has aroused our interest in conducting a comprehensive multi-scale study on this matter.

Desulfation of the accumulated SO<sub>x</sub> involves heating the catalyst to the temperature above 700°C or switching to a reducing atmosphere (CO or H<sub>2</sub>) [12-16]. The main issue for the high-temperature desulfation is the loss of the catalytic activity caused by thermal aging (precious metal sintering and formation of BaAl<sub>2</sub>O<sub>4</sub> [17]). Exposure to H<sub>2</sub> on the other hand deteriorates the storage material through formation of crystalline BaS [18].

In contrast to abundant experimental data focused on sulfur poisoning, no theoretical work fully assessing chemisorption of SO<sub>2</sub> or SO<sub>3</sub> has been conducted up to date. Most of the existing studies targeted SO<sub>x</sub> adsorption on alkaline-earth oxides at low surface coverage [19-22]. All of them unanimously agree that both SO<sub>2</sub> and SO<sub>3</sub> readily adsorb as Lewis acids by anchoring the sulfur atom to a basic oxygen site on BaO surface to form sulfite- (SO<sub>2</sub> adsorption) and sulfate-like (SO<sub>3</sub> adsorption) surface species. Our previous studies were focused on acquiring fundamental insight into the nature of SO<sub>3</sub> interactions with various types of BaO surfaces

(ideal surfaces and surface defects) at high surface coverages, providing a broader picture of SO<sub>x</sub> chemistry on BaO [23].

When it comes to kinetic models, there is a great need for developing reaction schemes based on quantified data for sulfur poisoning. Very few kinetic models for sulfur deactivation have been proposed in the literature. The most elaborated one, conceived by Dawody *et al.* [24] describes a multi-site competitive SO<sub>x</sub> adsorption on the NO<sub>x</sub> storage sites. According to their model, SO<sub>2</sub> is oxidized on Pt sites to SO<sub>3</sub> during the storage phase and reduced to H<sub>2</sub>S during the regeneration in the presence of H<sub>2</sub>. In a more recent modeling study by Olsson *et al.* [25] sulfur poisoning is described *via* SO<sub>2</sub> adsorption on BaO and Al<sub>2</sub>O<sub>3</sub> and the subsequent oxidation to sulfate species.

Multiscale modeling of heterogeneous chemical reactions implies transposing fundamental mechanistic insights that are available from molecular modeling (DFT, force-field) onto larger scales (kinetic Monte-Carlo, mean-field approximation) intended for catalyst design. Coupled to computational fluid dynamics models they provide powerful tools for reactor conception and design. A comprehensive review on multiscale modeling approaches in heterogeneous catalysis is available elsewhere [26].

The present study aims at bridging the gap between different modeling scales. The choice of the system to model in the present work is based on the reaction sequence for sulfate formation. We consider BaO to be the active storage site after surface BaCO<sub>3</sub> decomposition on which pre-oxidized SO<sub>3</sub> is adsorbed. Although substantial amounts of BaCO<sub>3</sub> and hydroxycarbonate coexist in equilibrium with BaO when storage material is exposed to engine exhaust, BaCO<sub>3</sub> does not act as the active storage phase on its own. Instead, detailed storage mechanisms involve CO<sub>2</sub> desorption prior to reaction with NO<sub>x</sub> or SO<sub>x</sub>. This is the motivation to consider BaO surface sites as chemically active ones in the present study.

We employed state-of-the-art Density Functional Theory (DFT) computations to obtain quantum insights on BaO–SO<sub>3</sub> interactions together with thermodynamic data that are not available in the literature. This information was used for conceiving kinetic model for SO<sub>3</sub> adsorption on BaO, implemented in the *IFP Exhaust* library. Our objective was testing the methodology of multiscale modeling in which DFT-based data obtained at the atomic level were used directly on a higher-level scale for conceiving kinetic models. As a final step, sensitivity analyses were performed to assess the importance of various modeling parameters to the sulfation mechanism.

## 1 METHODS

### 1.1 *Ab Initio* Computations

Periodic DFT calculations were carried out in the framework of the generalized gradient approximation exchange-correlation functional of Perdew and Wang PW91 [27], as implemented in VASP 4.6 package [28, 29]. The one-electron wave function was developed in a plane-wave basis set, and the interaction between core and valence electrons was described by the Projector Augmented Waves (PAW) approach [30]. A cutoff energy of 400 eV was used. The convergence criterion for the electronic Self-Consistent Field (SCF) loop is set to  $1 \times 10^{-6}$  eV per cell for simple structures (gas-phase molecules and solid bulks) or to  $5 \times 10^{-6}$  eV for supercell computations. Geometry optimizations were performed within a conjugate-gradient algorithm until the convergence criterion on forces ( $0.02 \text{ eV} \cdot \text{\AA}^{-1}$ ) was reached. A dipolar correction along the direction perpendicular to the slab (*z*-axis) was applied for neutralizing any spurious electrostatic interaction between the slab and its periodic images, due to the asymmetric nature of the slabs.

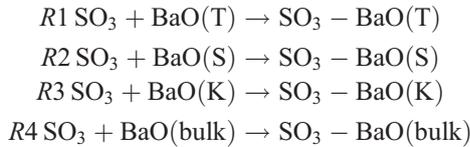
Velocity-scaled Molecular Dynamics (MD) were used for investigating species adsorption at higher fractional coverages, each time a surface reconstruction phenomenon was encountered. Velocities were scaled at each time step (5 fs) to the chosen temperature (600 K). The DFT calculation accuracy was decreased in order to limit computational cost. More precisely, a cutoff energy of 300 eV was used, with the convergence criterion for the electronic SCF loop set to  $1 \times 10^{-4}$  eV. The energetic minima obtained from the MD simulation were subsequently quenched by performing a geometry optimization at 0 K with usual accuracy parameters, and the most stable quenched structures are assumed to give the best estimate of the most energetically favorable configurations.

Raw *ab initio* data were used for quantifying the incremental stability of adsorbed states with the increasing SO<sub>3</sub> coverage (from  $(n - 1)$  to  $n$  adsorbed SO<sub>3</sub> molecules per cell) that we describe *via* differential adsorption energy,  $\Delta_{ads}U$ , defined as

$$\Delta_{ads}U = U_{\text{BaO} + n\text{SO}_3} - U_{\text{BaO} + (n-1)\text{SO}_3} - U_{\text{SO}_3} \quad (1)$$

where  $U_{\text{BaO} + (n-1)\text{SO}_3}$ ,  $U_{\text{BaO} + n\text{SO}_3}$  and  $U_{\text{SO}_3}$  are the energies of the adsorbed states and of SO<sub>3</sub> molecule, respectively. For the case of bulk BaSO<sub>4</sub> formation, the energy of formation is obtained by subtracting the calculated cohesive energy of BaSO<sub>4</sub> crystal from that of BaO and SO<sub>3</sub>.

In the present study, we focalize on SO<sub>3</sub> adsorption onto three types of surface sites – ideal BaO terraces (T) and two surface irregularities: surface steps (S) and kinks (K). Further information and detailed modeling parameters of the surfaces studied within is available from our previous work [23]. The fourth adsorption site considered is bulk BaO leading to the formation of crystalline BaSO<sub>4</sub>. This four-site reaction scheme is summarized below.



## 1.2 Kinetic Model

The proposed 4-site model supposes that the adsorbate is randomly distributed on each type of surface (mean-field assumption) [26]. Coverage dynamics of the adsorbed sulfur species on the surface site  $i$  is described *via* [31, 32]

$$\frac{d\theta_{\text{SO}_3,i}}{dt} = \frac{r_i}{\Psi_i} \quad (2)$$

in which  $r_i$  (mol·m<sup>-3</sup>·s<sup>-1</sup>) is the rate of consumption of generation of SO<sub>3</sub> due to adsorption or desorption onto/from  $i$ th site. Every site has its own density,  $\Psi_i$  (mol·m<sup>-3</sup>). Equation (3) describes the gaseous SO<sub>3</sub> source term,  $\omega_{\text{SO}_3}$

$$\omega_{\text{SO}_3} = M_{\text{SO}_3} V_{\Sigma} \sum_{i=1}^N r_i \quad (3)$$

in which  $N$  is the number of SO<sub>3</sub> storage site types,  $V_{\Sigma}$  is the active volume of the storage material, and  $M_{\text{SO}_3}$  is SO<sub>3</sub> molar weight. Reaction rates  $r_i$  are described by elementary step based reaction mechanisms. Forward reaction rate constants are described *via* the Arrhenius expression, and to assure the thermodynamic consistency of the model, the backward reactions are computed *via* the corresponding thermodynamic constants [33]

$$r_i = A_i \exp\left(-\frac{E_{a,i}}{RT}\right) \times \left(c_{\text{SO}_3} \theta_{\text{void},i} - \frac{1}{K_{eq,i}} \left(\frac{P}{RT}\right) \theta_{\text{SO}_3,i}\right) \quad (4)$$

with  $A_i$  being the pre-exponential factor,  $E_{a,i}$  the corresponding activation energy,  $c_{\text{SO}_3}$  is gas-phase SO<sub>3</sub> concentration,  $K_{eq,i}$  the thermodynamic equilibrium constant for adsorption on  $i$ th site. Site fractions  $\theta_{\text{void},i}$  and  $\theta_{\text{SO}_3,i}$  (dimensionless) describe void and SO<sub>3</sub> fractional coverage on  $i$ th site, respectively. The equilib-

rium constants are calculated from the corresponding thermodynamic data *via*

$$K_{eq,i} = \exp\left(-\frac{\Delta_r H_i}{RT}\right) \exp\left(\frac{\Delta_r S_i}{R}\right) \quad (5)$$

with  $\Delta_r H_i$  and  $\Delta_r S_i$  representing respectively the enthalpy and the entropy of the adsorption reaction on  $i$ th adsorption site.

## 1.3 Reactor Model

The kinetic scheme was implemented in a reactor model developed in the AMESim (LMS.Imagine.Lab) modeling platform, itself based on the bond-graph theory [34]. Briefly, the bond-graph approach associates capacitive elements (volume) and resistive elements (pressure drop, mass and enthalpy flow rates) for modeling multi-physical systems such as chemical reactors. Detailed architecture of the bond-graph reactor model we used is available elsewhere [35]. Its successful implementation in multi-0D kinetic modeling has been demonstrated in our previous work [36-38]. Species mass balance is computed as

$$\frac{dm_j}{dt} = \dot{m}_j^{\text{in}} - \dot{m}_j^{\text{out}} + \omega_j \quad (6)$$

in which  $\dot{m}_j^{\text{in}}$  and  $\dot{m}_j^{\text{out}}$  represent inlet and outlet mass flux for species  $j$  (SO<sub>3</sub> or the carrier gas), while  $\omega_j$  stands for the chemical source term (only applicable to SO<sub>3</sub>, Eq. 3). Note that the impact of internal transport was not taken into account in this study. In order to describe more accurately the LNT operation, the impact of internal porosity variation on the effective species diffusivity would have to be accounted for [39]. Pressure is calculated from the energy balance inside the reactor volume [35]

$$\frac{dP}{dt} = \frac{\gamma P}{m C_p T_g} \left( \delta \dot{Q}_{th,in} + M C_p T_g \frac{dn}{dt} + \dot{m} \delta h \right) \quad (7)$$

$\gamma$  being the isentropic coefficient,  $T_g$  gas temperature,  $C_p$  gas specific heat,  $n$  is the amount of gas,  $M$  its molar mass, and  $\delta \dot{Q}_{th,in}$  the internal heat transfer, calculated from the difference between gas- and solid-phase temperatures. The reactor is modeled as a fixed bed filled with BaO powder for which mass flux and superficial gas velocity  $v$  are computed from pressure drop across the bed using Darcy's law [40]

$$\frac{\Delta P}{L} = \frac{150(1-\epsilon)^2 \mu}{\epsilon^3 d_p^2} v \quad (8)$$

$\Delta P$  being the pressure drop,  $L$  the bed length,  $\epsilon$  the bed void fraction,  $\mu$  the dynamic viscosity of the fluid and  $dp$  the particle diameter.

## 2 RESULTS

### 2.1 SO<sub>3</sub> Adsorption on BaO: Quantum Mechanical Insights

In our previous DFT study, we thoroughly investigated SO<sub>3</sub> adsorption thermodynamics on several BaO surface types (terraces, steps and kink surface defects) [23]. It has been found, in line with previous theoretical studies, that SO<sub>3</sub> molecule adsorbs readily on basic oxygen surface sites. SO<sub>3</sub> acts as a multidentate ligand that tends to surround itself by a maximal number of coordination bonds with BaO. Site topology has been found to strongly influence the thermodynamics of the adsorption. When adsorbed, SO<sub>3</sub> molecule is strongly deformed from its original state, forming a tetrahedral environment of the S atom, characteristic of a sulfate-alike structure.

Once adsorbed on BaO surface, SO<sub>3</sub> molecule penetrates and restructures its environment to form bulk BaSO<sub>4</sub>. With an increasing surface coverage, reconstruction phenomena are observed for the terrace adsorption. Every time a surface reconstruction was encountered during a static geometry optimization, a molecular dynamic simulation was performed to explore possibilities for a further surface reconstructions. This was the case for SO<sub>3</sub> adsorption on terraces at surface coverages higher than 0.5 ML (monolayer). Calculated adsorption energies are illustrated as points in Figure 1. We showed previously that steps and kinks are not strongly reconstructed upon SO<sub>3</sub> adsorption, contrary to terraces. However, SO<sub>3</sub> adsorbs strongly on these surface defects, which suggests that diffusion of sulfates only involves the terraces [23].

Further investigations of SO<sub>3</sub> adsorption on BaO aimed to provide an insight into adsorption kinetics. This was achieved by tracing the energetic profile of a SO<sub>3</sub> molecule approaching a basic O<sub>5C</sub> site. For this purpose, the most stable sulfate structure obtained for the adsorption on a BaO(100) terrace was distorted by increasingly moving the molecule away from the surface along the  $z$  axis. The adsorption energy profile (Fig. 2) illustrates a transition from a physisorbed to a chemisorbed state. No noticeable activation barrier for a transition from the gas-phase SO<sub>3</sub> to a chemisorbed state was observed for this perpendicular approach. This finding is particularly interesting for the conception of the kinetic model, allowing us to postulate a non-activated surface SO<sub>3</sub> adsorption. Note finally that the reactivity – eventually

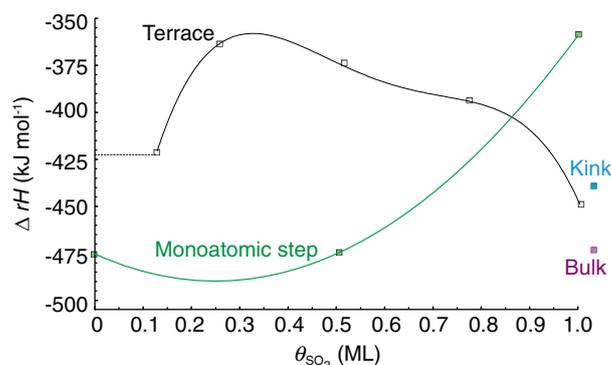


Figure 1

Standard (101.325 kPa, 298.15 K) SO<sub>3</sub> adsorption enthalpies ( $\Delta rH$ ) on various types of BaO sites (terraces, steps, kinks and bulk sites) as a function of SO<sub>3</sub> fractional coverage,  $\theta_{\text{SO}_3}$ . Points represent the results obtained from *ab initio* calculations, lines are the interpolations to all fractional coverage values.

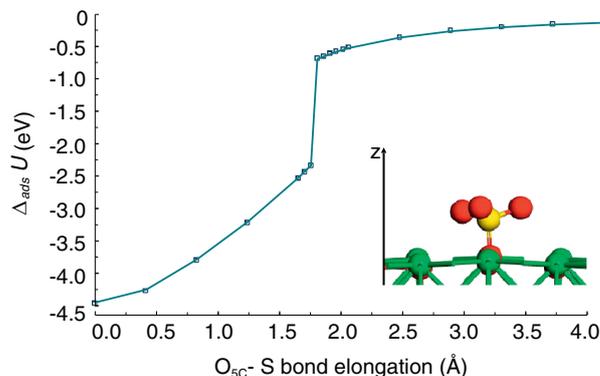


Figure 2

SO<sub>3</sub> molecule adsorbed onto a basic oxygen site of the BaO surface. Energetic profile for the SO<sub>3</sub>–BaO(100) system as the molecule approaches the basic surface site along the  $z$  axis. The bond elongation is relative to the equilibrium bond length of 1.57 Å.

migration – of surface oxygen atoms cannot be excluded, although it is not sufficient to explain the formation of bulk sulfate requiring S atoms. We are presently working on the interaction of O<sub>2</sub> and SO<sub>2</sub> with BaO, which should allow us to draw conclusions on the importance of the migration of peroxide at the surface.

### 2.2 Kinetic Study

Following our *ab initio* studies [23], we modeled SO<sub>3</sub> adsorption on three types of surface sites (terraces, steps

and kinks) and on bulk BaO site using a global modeling approach. Storage material was represented as a BaO particle with a storage capacity of  $3.89 \times 10^4 \text{ mol}\cdot\text{m}^{-3}$ , based on the elementary BaO cell volume of  $170.67 \text{ \AA}^3$  and four BaO formula units per cell. In line with BaO dispersions (around 33%) measured by XRD for a typical model Pt/Ba/Al<sub>2</sub>O<sub>3</sub> formulation [41], we consider that one third of the storage sites are surface sites, and the two thirds represent bulk BaO. To obtain the speciation of various surface sites, it is helpful to look at the values of surface energies relative to every kind of surface we are interested in. These values are available from our DFT studies [23] and we postulate the abundance of each surface site inversely proportional to its surface energy value (Fig. 3).

We used the thermodynamic data extracted from the *ab initio* studies, to conceive a kinetic model that describes SO<sub>3</sub> adsorption on BaO particle. First parameters that we discuss are the pre-exponential factors used for the global simulation. Surface adsorptions are modeled with a pre-exponential factor of  $1.0 \times 10^6 \text{ s}^{-1}$ , corresponding to a typical transition state theory-based value for an immobile precursor molecular adsorption [42]. The pre-exponential factor for adsorption on bulk BaO sites of  $1.0 \times 10^7 \text{ s}^{-1}$  was based on a typical value for a mobile precursor mediated adsorption, knowing that the formation of bulk sulfate commences with a surface adsorption, and therefore requires the molecule to diffuse into deeper layers. The value we discuss for bulk adsorption is relatively close to the one proposed in the study of Dawody *et al.* [24] for SO<sub>3</sub> adsorption on bulk site. The numerical value attributed by the authors is

$2.33 \times 10^4 \text{ m}^3\cdot\text{mol}^{-1}\cdot\text{s}^{-1}$  or, expressed as a turnover rate,  $9.1 \times 10^8 \text{ s}^{-1}$ .

Based on the non-activated approach of a SO<sub>3</sub> molecule to a basic O site (Fig. 2), activation energies for SO<sub>3</sub> adsorption on surfaces are kept at zero. Formation of bulk BaSO<sub>4</sub> however requires a SO<sub>3</sub> molecule to penetrate into the crystal structure. The activation energy proposed by Dawody *et al.* [10] ( $1 \text{ kJ}\cdot\text{mol}^{-1}$ ) seems fairly low for passing a barrier for breaking bulk Ba–O bonds inside the crystal structure. Instead, we propose a value of  $80.5 \text{ kJ}\cdot\text{mol}^{-1}$ , that is approximately 1/6 of the atomization energy of crystal BaO [43].

With the adsorption energies for each of the four sites in hand, we based all adsorption enthalpies solely on our previous DFT data [23]. Adsorption enthalpy  $\Delta rH$  is deduced directly from the corresponding adsorption energy,  $\Delta_{ads}U$  (Eq. 1) using the fundamental thermodynamic relation:

$$\Delta rH = \Delta_{ads}U + PV \quad (9)$$

where the term  $PV$  is substituted with  $RT$ , attributing all volume change due to the adsorption event to the volume of the adsorbed gas molecules. In other terms, the condensed phase volume variations are considered neglectable in front of the gas volume change.

For the case of SO<sub>3</sub> adsorption on terraces and steps, we worked out an entire range of adsorption energies as a function of SO<sub>3</sub> fractional coverage,  $\theta_{\text{SO}_3}$ . The values are extrapolated over the 0-1 ML fractional coverage range using an appropriate polynomial fit (Fig. 1, Tab. 1). Since the supercell model used in the periodic DFT approach contains eight surface Ba atoms, the lowest fractional coverage value we model is 1/8, or 0.125 ML. For the values below 0.125 ML, we confidently postulate no or very little lateral interactions between adsorbed molecules, and use the same adsorption enthalpy value from 0.125 ML to all lower coverages (Fig. 1, dashed line).

Adsorption entropies used in the global model are based on the estimation of the changes in the molecule's degrees of freedom during the adsorption event. Given the nature of SO<sub>3</sub> adsorption (non-activated and highly thermodynamically favorable), the adsorbed species may be described as a completely localized species. The entropy change between the gas phase and a localized species can be described by the following equation:

$$\Delta rS = -S_{tr,3D} - S_{rot,3D} \quad (10)$$

where  $S_{tr,3D}$  and  $S_{rot,3D}$  represent the translational and the rotational contribution to the entropy of SO<sub>3</sub> molecule in the gas phase, respectively. The thermochemistry

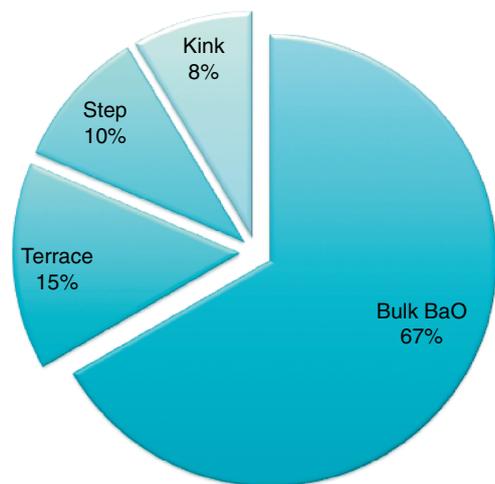


Figure 3  
Speciation of BaO sites used in global simulations.

TABLE 1  
Kinetic and thermodynamic parameters for SO<sub>3</sub> adsorption on different BaO sites

Site	Terrace	Step (S)	Kink (K)	Bulk
$A$ (s <sup>-1</sup> )	$1.0 \times 10^6$	$1.0 \times 10^6$	$1.0 \times 10^6$	$1 \times 10^7$
$E_a$ (kJ·mol <sup>-1</sup> )	0	0	0	80.5
$\Delta rH$ (kJ·mol <sup>-1</sup> )	-420 for $\theta_{\text{SO}_3} \leq 0.125$ ML and $-2587 \times \theta_{\text{SO}_3}^4 + 6175 \times \theta_{\text{SO}_3}^3 - 5294 \times \theta_{\text{SO}_3}^2 +$ $1836 \times \theta_{\text{SO}_3} - 579$ for $0.125 \text{ ML} < \theta_{\text{SO}_3} \leq 1$ ML	$232 \times \theta_{\text{SO}_3}^2$ $-116 \times \theta_{\text{SO}_3} - 475$	-469	-437
$\Delta rS$ (J·mol <sup>-1</sup> ·K <sup>-1</sup> )	-246	-246	-246	-314

of the SO<sub>3</sub> molecule in gas phase was determined thanks to the integration of partition functions, according to the ideal gas model, after a frequency mode determination performed with Dmol program (distributed by *Accelrys*). To the adsorption on a bulk site is attributed an entropy change based on the data extracted from *Outokumpu HSC Chemistry* (distributed by *Outokumpu Research Oy*). All  $\Delta rS$  values are postulated to be temperature-independent.

The kinetic model was tested in the experimental conditions summarized in Table 2. The storage material (BaO) is packed within a cylinder tube and exposed to a 200 ppm SO<sub>3</sub> inlet in He carrier gas at 25°C during 2 500 s. The storage phase is followed by a temperature ramp of 5°C min<sup>-1</sup> allowing stored SO<sub>3</sub> to desorb. Obtained SO<sub>3</sub> profile is given in Figure 4.

As seen from Figure 5, SO<sub>3</sub> desorption starts from 800°C, a temperature slightly higher than typical desulfation temperatures for Pt/Rh/BaO/CeO<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts [15]. A higher desulfation temperature can be expected given the fact that synergic effects between

noble metal and storage material may facilitate thermal decomposition of BaSO<sub>4</sub> [16]. To get a better insight into the desulfation kinetics, we followed reaction rates and surface coverages during the temperature ramp. Results given in Figure 6 reveal that, at room temperature, all surface sites are subject to poisoning, whereas bulk web-sites do not react yet. During the temperature increase and after having reached 620°C, SO<sub>3</sub> migrates from terrace sites toward void step and divacancy sites, resulting in an increase of their coverage values (*Fig. 7*). Migration from terrace sites continues at higher temperatures, conveying SO<sub>3</sub> to bulk sites. Simultaneously, but to a lesser extent, step sites also contribute to bulk BaSO<sub>4</sub> formation. The balance SO<sub>3</sub> desorbed from terraces is seen as a small, sharp peak at 780°C. According to our rate analysis, the peak in SO<sub>3</sub> signal at 985°C is a result of bulk desorption, superposed with minor contributions of terrace and step desorptions. The final two SO<sub>3</sub> signals arise from kink and step desorptions, respectively.

The evolution of surface and bulk saturation during the temperature ramp is consistent with the reaction rate

TABLE 2  
Modeled conditions and setup for SO<sub>3</sub> storage and TPD on BaO

Parameter	Value
Gas composition	Storage phase: 200 ppm SO <sub>3</sub> in He during 2 500 s TPD phase: He
Volumetric flow rate (SCCM)	$6.0 \times 10^3$
Reactor length (mm)	14.0
Reactor diameter (mm)	7.0
BaO volume (mm <sup>3</sup> )	216
BaO storage capacity (mol m <sup>-3</sup> )	$3.89 \times 10^4$
$T$ profile	Storage: 25°C TPD: 25-1 000°C ramp, 5°C·min <sup>-1</sup>

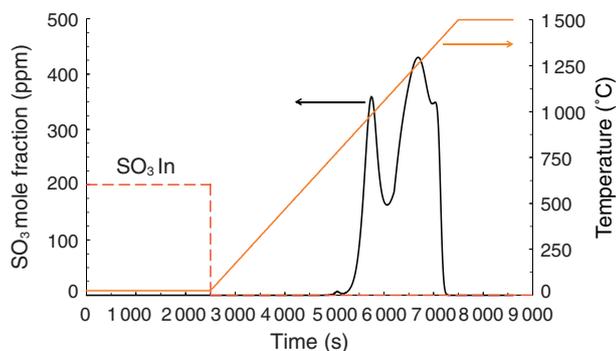


Figure 4

SO<sub>3</sub> inlet (red) and outlet (black) concentration profiles during the storage and temperature ramp experiment, in the conditions presented in Table 2. For illustration purposes, temperature profile is also given (orange).

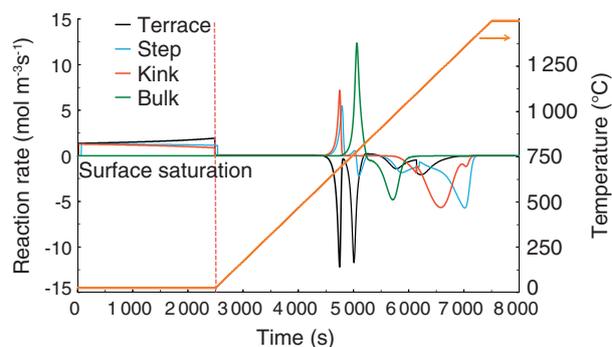


Figure 6

Reaction rates *versus* time during the storage-TPD experiment. The end of the SO<sub>3</sub> storage phase is delimited with a dashed line. Temperature profile is given in orange.

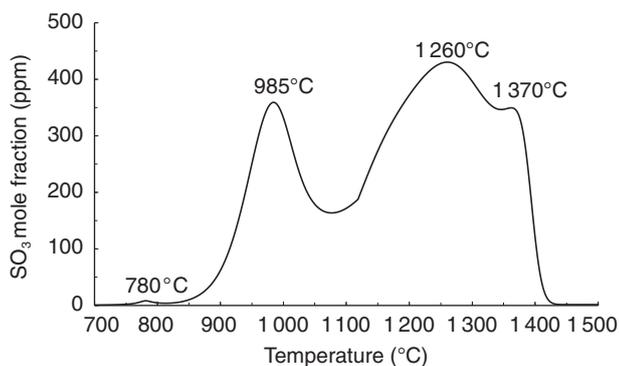


Figure 5

A closer look to the SO<sub>3</sub> outlet concentration profile *versus* temperature during the temperature ramp experiment.

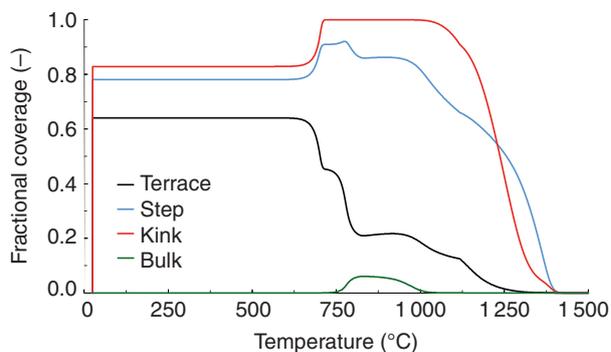


Figure 7

SO<sub>3</sub> fractional coverages as a function of temperature during the storage-TPD experiment.

analysis (Fig. 7). It can be seen that during the exposure to SO<sub>3</sub> at room temperature, three surface sites interact readily with SO<sub>3</sub>, and thus their fractional coverages reach values different from zero. The initial transfer of SO<sub>3</sub> from terrace to step and kink sites is observed above 620°C as the terrace coverage decreases with a simultaneous increase in the step and kink coverages. A subsequent transfer from terraces to bulk is marked as a sharp decrease in terrace coverage above 710°C leading to a formation of bulk BaSO<sub>4</sub>. As a final step of the desorption mechanism, on line with rate analyses, surface step and kink desulfation take place after bulk and terrace depopulation, liberating the last traces of SO<sub>3</sub>.

Further assessment of the storage-desorption mechanism was made available through sensitivity analyses performed on the parameters with the highest degree of uncertainty. The sensitivity analysis was done in the storage conditions similar to those in Table 2, but with 400 ppm SO<sub>3</sub> inlet during 2 500 s. The increase in SO<sub>3</sub> concentration from original 200 to 400 ppm was necessary to operate in excess of SO<sub>3</sub> so to saturate the storage material. This way, the total quantity of stored SO<sub>3</sub> obtained in different scenarios by increasing independently the original value of each parameter for 10% can be compared directly to the original storage scenario. The results are depicted in Figure 8. We were mainly interested in the parameters that we adopted from the literature

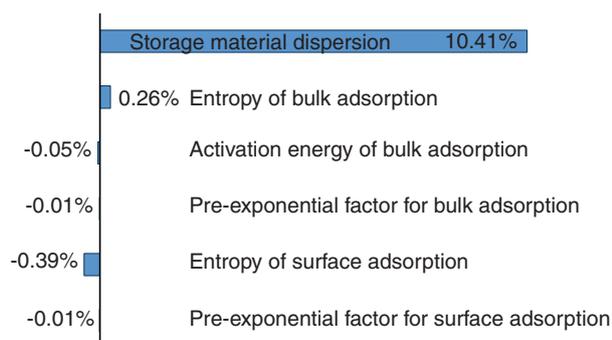


Figure 8

Results of the sensitivity studies for the storage of 400 ppm SO<sub>3</sub> over BaO during which various model parameters were successively increased for 10% and the quantity of stored SO<sub>3</sub> compared to that obtained in the original scenario.

(pre-exponential factors,  $A_i$ ) and in those that were estimated in Dmol (adsorption entropies,  $\Delta rS_i$ ). We also examined the impact of the storage material dispersion (*i.e.*, quantity of exposed surface sites as opposed to the total number of sites). Interestingly, the sensitivity analysis shows that in our conditions the dispersion has the greatest impact on the storage properties. The amount of stored SO<sub>3</sub> increases linearly with a dispersion increase. This leads to a conclusion that among all simulation parameters with a high degree of uncertainty, dispersion plays the most relevant role. Consequently, controlling BaO dispersion during catalyst preparation is of primary interest for sulfur storage properties.

## CONCLUSIONS

In summary, the multiscale modeling study presented in this paper was based on our previous work on SO<sub>3</sub> adsorption on BaO. Transposing the kinetic model proposed within as a part of the global picture into real engine exhaust operating conditions would require taking into account BaCO<sub>3</sub> formation and decomposition prior to sulfate formation to predict effectively the actual LNT operation. *Ab initio* quantum mechanical calculations were performed to elucidate the thermodynamics for SO<sub>3</sub> adsorption on BaO surfaces and bulk. We then focused on transposing the results of the *ab initio* calculations to a mean-field kinetic model implemented in *IFP Exhaust* library. The paper shows the main assumptions that have been made for overcoming the gap between the two scales. Further *ab initio* calculations could provide valuable kinetic data such as pre-exponential factors that were taken from the literature for the present study. This approach allows us to simulate SO<sub>3</sub> concentration

profile obtained in a TPD experiment subsequent to SO<sub>3</sub> storage. The analysis of the adsorption/desorption scenarios was made through comparing reaction rates and species fractional coverages. BaO(100) terraces were found to be at the crossroads of bulk sulfate formation and a SO<sub>3</sub> provider for surface defects.

Sensitivity analysis performed on the original storage scenario provided us a deeper insight into the most relevant kinetic factors. The dispersion of the BaO storage material turns out to be the most important parameter for SO<sub>3</sub> adsorption prediction. A comparison with experimental data would prove useful to better judge the validity of the kinetic model we proposed. Moreover, the thermokinetics of the reaction of O<sub>2</sub> and SO<sub>2</sub> (present in the exhaust stream) with BaO will be compared in the future to that of SO<sub>3</sub> adsorption in order to assess the actual contribution of these steps to sulfate formation. Kinetic modeling stands for an appropriate tool to identify the preferential pathway.

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