

# Exergetic Evaluation of Speed and Load Effects in Spark Ignition Engines

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**Résumé — Évaluation exergetique des effets de la vitesse et de la charge dans les moteurs à allumage par étincelle** — Cette étude examine les effets des différentes conditions de fonctionnement de moteurs à allumage commandé via une analyse exergetique. Un modèle de cycle thermodynamique comprenant les processus de compression, combustion et détente a été utilisé. Les processus d'admission et d'échappement sont modélisés à l'aide d'une méthode simple d'approximation. Les principes de la deuxième loi de la thermodynamique ont été appliqués au modèle de cycle pour effectuer l'analyse exergetique. Des variables exergetiques comme les transferts exergetiques de chaleur et de travail, les irréversibilités, l'exergie thermomécanique, l'exergie chimique du carburant et l'exergie totale ont été calculées dans l'analyse exergetique. La variation des paramètres exergetiques et leur distribution dans l'exergie du combustible ont été déterminées pour différentes conditions de fonctionnement, c'est à dire différentes vitesses du moteur et différentes charges. L'efficacité déduite, d'une part, de la première et la deuxième loi de la thermodynamique et, d'autre part, de la consommation spécifique de carburant ont également été calculées pour révéler les conditions optimales de fonctionnement. Les résultats montrent que le transfert exergetique de chaleur diminue et que le transfert exergetique par l'échappement augmente avec la vitesse du moteur. Le régime moteur de 3 000 tr/min donne le transfert d'exergie maximal de travail, les irréversibilités minimales, les meilleurs rendements et la moindre consommation de carburant. Les transferts exergetiques avec la chaleur, le travail et l'échappement et ainsi que les irréversibilités augmentent avec la charge du moteur. En outre, l'efficacité déduite de la première et la seconde loi de la thermodynamique augmente et la consommation de carburant diminue avec la charge du moteur, donc une charge du moteur élevée donne les meilleurs rendements et la moindre consommation de carburant.

**Abstract — Exergetic Evaluation of Speed and Load Effects in Spark Ignition Engines** — This study investigates the effects of various operating conditions in spark ignition engines via an exergy analysis. A thermodynamic cycle model including compression, combustion and expansion processes was used for investigation. Induction and exhaust processes were computed with a simple approximation method. The principles of the second law were applied to the cycle model to perform the exergy analysis. Exergetic variables, i.e., the exergy transfers with heat and work, irreversibilities, thermomechanical exergy, fuel chemical exergy and total exergy were calculated in the exergy analysis. Variation of the exergetic parameters and the distribution of them into the fuel exergy were determined for various operating conditions, i.e., engine speed and load. The first and second law efficiencies and specific fuel consumption were also computed to reveal the optimum operating conditions. The results show that the exergy transfer with heat decreases and the exergy transfer with exhaust gases increases with increasing engine speed. Engine speed of 3 000 rpm gives the maximum exergy transfer as work, the minimum irreversibility and the best efficiency and fuel consumption. Exergy transfers with heat, work and exhaust and irreversibilities increase with increasing engine load. Additionally, the first and second law efficiencies increase and fuel consumption decreases with increasing engine load, so a high engine load gives the best efficiency and fuel consumption.

**NOMENCLATURE**

$A$	Availability or exergy (J)
$a$	Specific availability or exergy (J/kg)
$b$	Bore (m)
$BMEP$	Brake Mean Effective Pressure (bar)
$BSFC$	Brake Specific Fuel Consumption (bar)
$c_p$	Specific heat at constant pressure (J/kg K)
$E$	Energy (J)
$F$	Surface (m <sup>2</sup> )
$FMEP$	Friction Mean Effective Pressure (bar)
$h$	Specific enthalpy (J/kg)
$I$	Irreversibility (J)
$IMEP$	Indicated Mean Effective Pressure (bar)
$L$	Length (m)
$m$	Mass (kg)
$n$	Engine speed (rpm)
$p$	Pressure (bar)
$P$	Power (kW)
$Q$	Heat transfer (J)
$Q_{LHV}$	Lower heating value of fuel (J/kg)
$r_c$	Compression ratio (dimensionless)
$S$	Entropy (J/K)
$s$	Specific entropy (J/kg K)
$T$	Absolute temperature (K)
$U$	Internal energy (J)
$u$	Specific internal energy (J/kg)
$V$	Volume (m <sup>3</sup> )
$v$	Specific volume (m <sup>3</sup> /kg)
$W$	Work (J)
$x_b$	Burned mass fraction (dimensionless)
$x_r$	Residual gas fraction (dimensionless)
$Z$	Number of cylinder (dimensionless)

**Greek Letters**

$\Phi$	Charge-up efficiency (%)
$\varepsilon$	Error (dimensionless)
$\phi$	Fuel air equivalence ratio (dimensionless)
$\eta_I$	The first law efficiency (%)
$\eta_{II}$	The second law efficiency (%)
$\eta_{vol}$	Volumetric efficiency (%)
$\lambda$	Heat transfer coefficient (W/m <sup>2</sup> K)
$\mu$	Chemical potential (J)
$\theta$	Crank angle (CAD)
$\theta_{st}$	Spark timing angle (CAD)
$\Delta\theta_b$	Burn duration (CAD)
$\sigma$	Total entropy generation (J)
$\omega$	Angular velocity (rad/s)

**Subscripts**

0	Reference or dead-state conditions
b	Burned
ch	Chemical
clr	Clearance
cr	Connecting rod
comb	Combustion
conv	Convection
d	Displacement
dest	Destruction
e	Effective (brake)
exh	Exhaust
f	Fuel
g	Gas
IVC	Intake valve closed
i	Indicated
in	Intake or inlet
kin	Kinetic
max	Maximum
pot	Potential
Q	Heat
r	Residual
s	Stroke
tm	Thermomechanical
tot	Total
toc	Temperature of coolant
u	Unburned
w	Wall
W	Work

**Superscripts**

$\cdot$	Derivation to the crank angle (d/d $\theta$ )
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**Abbreviation**

CAD	Crank Angle Degree
MBT	Maximum Brake Torque
ICE	Internal Combustion Engine

**INTRODUCTION**

Extremely complex physical and chemical events occur during Internal Combustion Engine (ICE) operation. Variation of engine operating parameters such as the fuel-air equivalence ratio, spark timing, engine speed and engine load noticeably influence these events and also all performance parameters of an engine [1]. Engine cycle models are very suitable tools to investigate the effects of such parameters and also to evaluate the engine performance [1, 2]. Cycle models of ICEs can be classified into two groups based on thermodynamics and

fluid mechanics [2-5]. The thermodynamic cycle models were created in the 1960s and they are commonly used nowadays in both industry and academia due to the fact that they are economical and do not require high computer capacity or extensive operation time [6, 7]. Additionally, only the first law of thermodynamics has been used in most of the work performed with the thermodynamic cycle models until now. However, the first law of thermodynamics is not adequate to study in detail the events relating to ICEs [7-10]. Therefore, the use of the second law of thermodynamics has intensified in the studies devoted to ICEs in recent times. Investigation of systems or processes by means of the second law of thermodynamics is called second law or exergy analysis. Exergy gives a quantitative and illustrative description of the convertibility of different energy forms. As is known, the processes in all real energy conversion systems are irreversible and a part of the exergy supplied to the total system is destroyed. The concept of exergy is extremely useful for the identification of the losses and irreversibility in the system by providing a more detailed tracking mechanism for the energy usage [9-12]. The real inefficiencies of a system are exergy destruction, occurring within the system boundaries and exergy losses, which are exergy transfers out of the system that are not further used in the overall system. For example, the exergy losses because of the friction, heat transfer and exhaust process and also irreversibilities sourced from the fluid motions, mixture formation, heat transfer and combustion phenomena can be determined by means of exergy analysis in ICEs, unlike an energy analysis. Thus, more efficient systems can be designed or performance of a present system can be improved by reducing the inefficiencies in the existing system. However, studies based on exergy analysis in the field of ICEs are limited compared with other ones. One of the previous studies devoted to exergy analysis of ICEs was performed by Traupel in 1957 [13]. Another previous study was completed by Patterson in 1962 [14]. Additionally, a series of studies on the application of exergy analysis to ICEs was carried out in the 1980s [15-19] and work on ICEs on the subject of exergy or the second law analysis has continued progressively in recent years [20-25]. In the present study, the effects of engine operating parameters such as engine speed and load are investigated via exergy analysis. To meet this goal, a thermodynamic cycle model originally developed by Ferguson [26] is adapted and used. The details of the cycle model and exergy analysis are given in the following section.

## 1 MATHEMATICAL MODEL

### 1.1 Governing Equations of Cycle Model

The governing equations of the cycle model are derived from the first law of thermodynamics (the energy equation) by

assuming that cylinder content obeys the ideal gas law. The differential form of the first law is as follows for a closed system, *i.e.*, engine cylinder [26, 27]:

$$\dot{u} m + \dot{m} u = \dot{Q} - p \dot{V} \quad (1)$$

Equation (1) shows that variation of the thermodynamic properties respects the crank angle. These thermodynamic properties are also functions of temperature and pressure. The following differential equations are used to determine cylinder pressure and burned and unburned gas temperatures through the simulation:

$$\dot{p} = \frac{A + B + C}{D + E} \quad (2)$$

here:

$$A = \frac{\dot{V}}{m}$$

$$B = \frac{\lambda_{\text{conv}}}{\omega m} \left[ F_b \left( 1 - \frac{T_w}{T_b} \right) \frac{v_b}{c_{p,b}} \frac{\partial \ln v_b}{\partial \ln T_b} + F_u \left( 1 - \frac{T_w}{T_u} \right) \frac{v_u}{c_{p,u}} \frac{\partial \ln v_u}{\partial \ln T_u} \right]$$

$$C = -(v_b - v_u) \dot{x}_b - v_b \frac{h_b - h_u}{c_{p,b} T_b} \dot{x}_b \frac{\partial \ln v_b}{\partial \ln T_b}$$

$$D = x_b \left[ \frac{v_b^2}{c_{p,b} T_b} \left( \frac{\partial \ln v_b}{\partial \ln T_b} \right)^2 + \frac{v_b}{p} \frac{\partial \ln v_b}{\partial \ln p} \right]$$

$$E = (1 - x_b) \left[ \frac{v_u^2}{c_{p,u} T_u} \left( \frac{\partial \ln v_u}{\partial \ln T_u} \right)^2 + \frac{v_u}{p} \frac{\partial \ln v_u}{\partial \ln p} \right]$$

and:

$$\dot{T}_b = \frac{-\lambda_{\text{conv}} F_b (T_b - T_w)}{\omega m x_b c_{p,b}} + \frac{v_b}{c_{p,b}} \frac{\partial \ln v_b}{\partial \ln T_b} \dot{p} + \frac{h_u - h_b}{x_b c_{p,b}} \dot{x}_b \quad (3)$$

$$\dot{T}_u = \frac{-\lambda_{\text{conv}} F_u (T_u - T_w)}{\omega m (1 - x_b) c_{p,u}} + \frac{v_u}{c_{p,u}} \frac{\partial \ln v_u}{\partial \ln T_u} \dot{p} \quad (4)$$

The instantaneous volume of the cylinder is also determined as:

$$V = V_{\text{clr}} \left\{ 1 + \frac{r_c - 1}{2} \left[ 1 - \cos \theta + \frac{1}{\chi} \alpha \right] \right\} \quad (5)$$

In Equation (5):

$$\chi = L_s / 2 L_{\text{cr}}$$

$$\alpha = 1 - (1 - \chi^2 \sin^2 \theta)^{1/2}$$

here,  $L_s$  and  $L_{\text{cr}}$  are stroke and connecting rod length, respectively. One can easily derive the  $dV/d\theta$  from Equation (5).

The following differential equations are also used to determine indicated work and heat loss:

$$\dot{W} = p \dot{V} \quad (6)$$

$$\dot{Q}_L = \frac{\lambda_{\text{conv}}}{\omega} \left[ F_b (T_b - T_w) + F_u (T_u - T_w) \right] \quad (7)$$

here,  $\omega$  is the angular speed of the crankshaft that can be determined as:

$$\omega = \frac{2 \pi n}{60} \quad (8)$$

In the equations above,  $\lambda_{\text{conv}}$ , the convective heat transfer coefficient, is determined from the Woschni correlation as follows:

$$\lambda_{\text{conv}} = 3.26 b^{-0.2} p^{0.8} T^{-0.55} w^{0.8} \quad (9)$$

In Equation (9),  $w$  is average gas velocity, which is determined from:

$$w = c_1 \bar{S}_p + c_2 \frac{V_d T_{\text{IVC}}}{P_{\text{IVC}} V_{\text{IVC}}} (p - p_m) \quad (10)$$

here,  $\bar{S}_p$  and  $p_m$  are mean piston speed and motored pressure and  $c_1$  and  $c_2$  are constants. During compression  $c_1 = 2.28$  and  $c_2 = 0$ ; and during combustion and expansion  $c_1 = 2.28$  and  $c_2 = 3.24 \times 10^{-3}$  were used.

The cylinder wall temperature in the equations above is determined as follows [28]:

$$T_w = T_{\text{toc}} + R_w \dot{Q} \quad (11)$$

here,  $T_{\text{toc}}$  and  $R_w$  are the temperature of the coolant and conductive resistance of the cylinder wall, respectively.  $T_{\text{toc}} = 350$  K and  $R_w \cong 0.01$  K/W were used during simulation.

As is known, a Spark Ignition (SI) engine cycle consists of four consecutive processes: intake, compression, expansion (including combustion) and exhaust. In this study, the intake and exhaust processes are computed by using an approximation method [2]. In this method, the pressure and temperature of the intake process and volumetric efficiency are determined as follows:

$$p_{\text{in}} = p_0 - \Delta p_{\text{in}} \quad (12)$$

$$T_{\text{in}} = \frac{T_0 + \Delta T + x_r T_r}{1 + x_r} \quad (13)$$

$$\eta_{\text{vol}} = \Phi \frac{r_c}{r_c - 1} \frac{p_{\text{in}}}{p_0} \frac{T_0}{T_{\text{in}} (1 + x_r)} \quad (14)$$

here,  $\Delta p_{\text{in}}$  is pressure loss, which is determined from the Bernoulli equation for one-dimensional incompressible flow,  $\Delta T$  is the increase in charge temperature throughout the intake system,  $T_r$  is the exhaust temperature in the previous cycle and  $x_r$  is the residual gas coefficient.  $\Phi$  is also the charge-up efficiency which is determined from:

$$\Phi = 3.39 \times 10^{-5} n + 0.9163$$

Compression and expansion processes were computed from the governing equations of Equations (2-7) by the arrangement of them for each process in a suitable manner. The adiabatic flame temperature is assumed as the start of combustion temperature and the mass burning rate is computed from the cosine burn rate equation:

$$x_b = \frac{m_b}{m_{\text{tot}}} = \frac{1}{2} \left\{ 1 - \cos \left( \frac{\pi (\theta - \theta_{\text{st}})}{\Delta \theta_b} \right) \right\} \quad (15)$$

In Equation (15),  $\theta_{\text{st}}$  is spark timing and  $\Delta \theta_b$  is burn duration, which is determined for certain operating parameters by using the following empirical correlations [29]:

$$f_1(r_c) = 3.2989 - 3.3612 (r_c/r_{c1}) + 1.0800 (r_c/r_{c1})^2$$

$$f_2(n) = 0.1222 + 0.9717 (n/n_1) - 0.05051 (n/n_1)^2$$

$$f_3(\phi) = 4.3111 - 5.6383 (\phi/\phi_1) + 2.3040 (\phi/\phi_1)^2 \quad (16)$$

$$f_4(\theta_{\text{st}}) = 1.0685 - 0.2902 (\theta_{\text{st}}/\theta_{\text{st}1}) + 0.2545 (\theta_{\text{st}}/\theta_{\text{st}1})^2$$

$$\Delta \theta_b(r_c, n, \phi, \theta_{\text{st}}) = f_1(r_c) f_2(n) f_3(\phi) f_4(\theta_{\text{st}}) \Delta \theta_{b1} \quad (17)$$

here,  $\Delta \theta_{b1}$  is the known combustion duration for the operating conditions of  $r_{c1}$ ,  $n_1$ ,  $\phi_1$  and  $\theta_{\text{st}1}$ . The  $\Delta \theta_{b1}$  is 24 CAD when the baseline conditions are taken as  $r_{c1} = 7.5$ ,  $n_1 = 1000$  rpm,  $\phi_1 = 1.0$ , and  $\theta_{\text{st}1} = -30$  CAD. Thus,  $\Delta \theta_b$  is easily determined for the specified operating parameters.

The pressure and temperature for the exhaust process are also computed by using an approximation method [2]:

$$p_{\text{exh}} = c p_0 \quad (18)$$

$$T_{\text{exh}} = \frac{T_b}{(p_b/p_{\text{exh}})^{1/3}} \quad (19)$$

here,  $c$  is a constant between 1.05 and 1.25;  $p_b$  and  $T_b$  is the final pressure and temperature of combustion. Further details of the cycle model can be found in references [26, 27].

## 1.2 Engine Performance Parameters

The engine performance parameters are determined from the widely known relations given below. Indicated and Brake Mean Effective Pressure are defined as follows:

$$IMEP = \frac{W_i}{V_d} \quad (20)$$

here,  $W_i$  is the indicated work output and  $V_d$  is displacement volume of a single cylinder:

$$BMEP = IMEP - FMEP \quad (21)$$

here,  $FMEP$  is the Friction Mean Effective Pressure, which is determined following a modified Barnes-Moss correlation for gasoline or SI engines:

$$FMEP = 0.6 + (1.167 \times 10^{-4} n) + 0.06 \bar{S}_p \quad (22)$$

The brake power is defined as:

$$P_e = \frac{BMEP V_d n Z}{k 60} \quad (23)$$

here,  $k$  is a constant which is 1 for two-stroke engines and 2 for four-stroke engines.

The first law (or energy-based) efficiency is defined as [7, 9, 10]:

$$\eta_{li} = \frac{\text{Energy out (as work)}}{\text{Energy in}} = \frac{W_i}{m_f Q_{LHV}} \quad (24)$$

here,  $m_f$  is the absolute mass of inducted fuel and  $Q_{LHV}$  is the lower heating value of the fuel.

Brake Specific Fuel Consumption is determined as:

$$BSFC = \frac{3600m_f}{P_e} \quad (25)$$

### 1.3 Governing Equations for Exergy Analysis

The second law is analogous to the statement of entropy balance as follows [7, 9, 10]:

$$\Delta S = \int (Q/T)_{\text{boundary}} + \sigma \quad (26)$$

here,  $\sigma$  is the total entropy generation due to the internal irreversibilities.

Considering the combination of the first and second laws of thermodynamics the availability (or exergy) equation can be written for a closed system as [7, 9, 10]:

$$A = E + p_0 V - T_0 S \quad (27)$$

here,  $E$  is the total energy, which is a sum of the internal, kinetic and potential energies ( $E_{\text{tot}} = U + E_{\text{kin}} + E_{\text{pot}}$ ).

Exergy is defined as the maximum theoretical work that can be obtained from a combined system (combination of a system and its reference environment) when the system comes into equilibrium (thermally, mechanically and chemically) with the environment. The maximum available work from a system emerges as the sum of two contributions: thermomechanical exergy,  $A_{\text{tm}}$ , and chemical exergy,  $A_{\text{ch}}$ . Thermomechanical exergy is defined as the maximum extractable work from the combined system, as the system comes into thermal and mechanical equilibrium with the environment, and it is determined as [7, 9-12]:

$$A_{\text{tm}} = E + p_0 V - T_0 S - \sum \mu_{0,i} m_i \quad (28)$$

here,  $m_i$  and  $\mu_{0,i}$  are the mass and chemical potential of species  $i$  calculated in restricted dead-state conditions.

In the restricted dead-state conditions, the system is in thermal and mechanical equilibrium with the environment and no work potential exists between the system and environment because of temperature and pressure differences. However, the system does not reach chemical equilibrium with the environment because the contents of the system are not permitted to mix with the environment or enter the chemical reaction by environmental components [30]. The difference between the compositions of the system in the restricted dead-state conditions and the environment can be used to obtain additional work, to reach chemical equilibrium. The maximum

work obtained in this way is called the chemical exergy which can be determined from [7, 9-12, 30]:

$$A_{\text{ch}} = \sum m_i (\mu_{0,i} - \mu_i^0) \quad (29)$$

here,  $\mu_i^0$  is the chemical potential of species  $i$  calculated in true dead-state conditions.

The exergy balance in any process for a closed system can also be written as [23]:

$$\Delta A = A_2 - A_1 = A_Q - A_W - A_{\text{dest}} \quad (30)$$

here,  $\Delta A$  is the variation of the total system exergy,  $A_2$  is the total exergy at the end of the process,  $A_1$  is the total exergy at the start of the process,  $A_Q$  is the exergy transfer by heat interactions,  $A_W$  is the exergy transfer with work interactions, and  $A_{\text{dest}}$  is the destroyed exergy through an irreversible process.

The exergy balance for an engine cylinder can also be written by considering the fuel chemical exergy [27, 31]:

$$\dot{A} = \left(1 - \frac{T_0}{T}\right) \dot{Q} - (\dot{W} - p_0 \dot{V}) + m_f a_{f,\text{ch}} \dot{x}_b - \dot{I}_{\text{comb}} \quad (31)$$

The left-hand side of Equation (31) refers to the rate of change in the total exergy in the cylinder. Thus, the total exergy of the cylinder content can be calculated from Equation (31) at any time and the exergy losses with exhaust gases can also be easily determined as the exergy remains in the cylinder at the end of the expansion period. The first and second terms on the right-hand side indicate exergy transfers with heat and work interactions. The third term on the right-hand side corresponds to the burned fuel exergy; here,  $a_{f,\text{ch}}$  is the fuel chemical exergy.  $a_{f,\text{ch}}$  is calculated by using the following equation for liquid fuels [32]:

$$A_{f,\text{ch}} = m_f a_{f,\text{ch}} = m_f Q_{LHV} \left[ 1.0401 + 0.01728 \frac{h'}{c'} + 0.0432 \frac{o'}{c'} + 0.2196 \frac{s'}{c'} \left( 1 - 2.0628 \frac{h'}{c'} \right) \right] \quad (32)$$

here,  $Q_{LHV}$  is the lower heating value of fuel, which is calculated by using Mendelyev's formula:

$$Q_{LHV} = 33.91 c' + 125.6 h' - 10.89 (o' - s') - 2.51 (9 h' - w') \quad (33)$$

The quantities  $h'$ ,  $c'$ ,  $o'$ ,  $s'$  and  $w'$  in Equations (32, 33) represent the mass fractions of the elements carbon, hydrogen and oxygen, the sulfur and water contents in the fuel, respectively.

The last term on the right-hand side of Equation (31) illustrates exergy destruction in the cylinder due to combustion. It is calculated as:

$$\dot{I}_{\text{comb}} = T_0 \dot{S}_{\text{comb}} \quad (34)$$

here,  $\dot{S}_{\text{comb}}$  is the rate of entropy generation due to combustion irreversibilities. It is calculated from a two-zone combustion model of entropy balance as [27, 31]:

$$\dot{S}_{\text{comb}} = \frac{d(m_b s_b)}{d\theta} + \frac{d(m_u s_u)}{d\theta} \quad (35)$$

here,  $m_b$  and  $m_u$  are the burned and unburned masses of the cylinder contents, and  $s_b$  and  $s_u$  are the entropy values of the burned and unburned gases.

Additionally, exergy destruction due to heat transfer irreversibilities is defined as follows:

$$\dot{I}_Q = T_0 \dot{S}_Q \quad (36)$$

Entropy production sourced from the heat transfer process is calculated as in Equation (37):

$$\dot{S}_Q = \frac{\dot{Q}_b}{T_b} + \frac{\dot{Q}_u}{T_u} \quad (37)$$

here,  $\dot{Q}_b$  and  $\dot{Q}_u$  are the rates of heat loss from burned and unburned gas zones at temperatures  $T_b$  and  $T_u$ , respectively.

Thus, the total irreversibilities can be calculated as:

$$\dot{I}_{\text{tot}} = \dot{I}_{\text{comb}} + \dot{I}_Q \quad (38)$$

Various of the second law efficiencies (exergetic or availability efficiency, or effectiveness) are defined in the literature [7, 27, 31]. The following definition is used in this study:

$$\eta_{\text{II}} = \frac{\text{Exergy out (as work)}}{\text{Exergy in}} = \frac{A_w}{m_f a_{f,\text{ch}}} \quad (39)$$

Finally, the dead-state conditions were taken as  $p_0 = 1$  atm and  $T_0 = 25^\circ\text{C}$  for exergy analysis.

## 2 NUMERICAL APPLICATIONS

### 2.1 Computer Program and Solution Procedure

A computer code was written in Fortran to perform the numerical applications. Once the intake conditions are defined, the thermodynamic state of the cylinder charge can be predicted by solving the governing differential equations of the cycle model. The Dverk subroutine is used to integrate the differential equations. The composition and thermodynamic properties of the unburned and burned cylinder contents are computed by using the Fortran subroutines, FARG (Fuel-Air-Residual Gas) and ECP (Equilibrium-Combustion-Products). Exergetic calculations are performed simultaneously, depending on the thermodynamic state of the cylinder contents. Finally, the results obtained can be corrected as follows [26]:

$$\varepsilon_1 = 1 - v m/V \quad (40)$$

$$\varepsilon_2 = 1 + W/\Delta(mu) + Q \quad (41)$$

The validity of the computer program is fulfilled by fixing the values of  $\varepsilon_1$  and  $\varepsilon_2$  at the  $10^{-4}$ .

### 2.2 Model Validity

For the validation of the cycle model, the predictions from the model were compared with experimental data obtained

TABLE 1

Specifications of the engines

Engines	$r_c$ (-)	$B$ (mm)	$L_s$ (mm)	$L_{cr}$ (mm)	$Z$ (-)	$V_d$ (L)
Engine I [33]	10	84.5	89	180	4	2
Engine II [34]	10	80.6	88	176	4	1.8
Engine III [35]	8	84	71.5	142	4	1.6

from the literature [33-35] for the conditions specified in Figure 1 and the engine specifications given in Table 1. The predictions are generally in good agreement with the experimental data as seen in Figure 1. The deviations are about 0.2-9.1% for pressure in Figure 1a, 1.2-30.5% for the mass fraction burned in Figure 1b, 0-0.8% for Brake Specific Fuel Consumption in Figure 1c, 0.9-5.4% for the second law (exergetic) efficiency in Figure 1d, 0-11.2% for exergy loss with heat flow rate in Figure 1e and 11.9-19.8% for exhaust exergy in Figure 1f. Thus, it can be said that the model has a sufficient level of confidence for parametric investigation.

## 3 RESULTS AND DISCUSSION

In this section, the differences between energy and exergy analysis are emphasized initially, and then the parametric exergy analysis is performed. Exergy analysis makes possible the identification of various exergy losses thanks to the friction, heat interaction and exhaust process and irreversibilities sourced from the fluid motions, mixture formation, heat transfer interaction and combustion phenomena, unlike an energy analysis, as mentioned in the Introduction. This situation can be clearly seen in Figure 2, which shows the results obtained from energy and exergy analysis for the specified conditions. As seen in Figure 2a and c, the irreversibilities can only be determined with the exergy analysis. Here, the irreversibilities arising from the heat interaction and combustion process are taken into consideration. In Figure 2b and d, there are also significant quantitative differences between the portions of the losses with heat interaction and exhaust and work output determined by means of energy and exergy analysis. The differences are about 3.81% for heat interaction, 2.85% for work interaction and 12.47% for exhaust losses. The sum of these differences is about 19.13%, which corresponds to the irreversibilities computed from exergy analysis as seen in Figure 2d. The results show that the differences that cannot be ignored between energy and exergy analysis require the exergy analysis to improve the design and/or operation of the system by identifying the losses and irreversibilities in a realistic way. On the other hand, parametric exergy analysis was performed in this study for the engine specifications [33] given in Table 1. The variation of exergetic variables with engine speed is given in Figure 3a-f. Exergy transfer with heat ( $A_Q$ ) decreases with increasing engine speed, as seen in Figure 3a. This variation can be

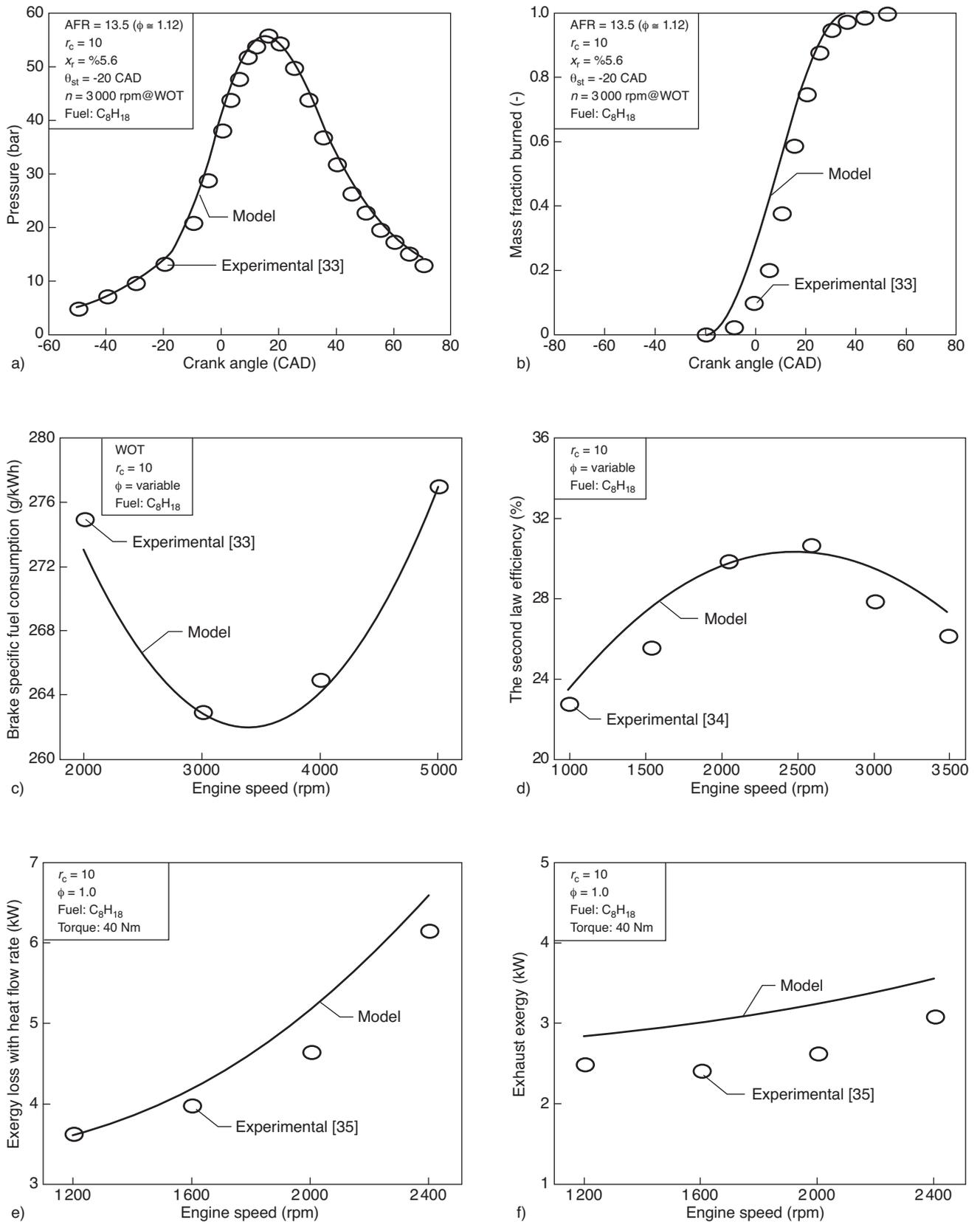


Figure 1  
 Comparison of various predicted and experimental data.

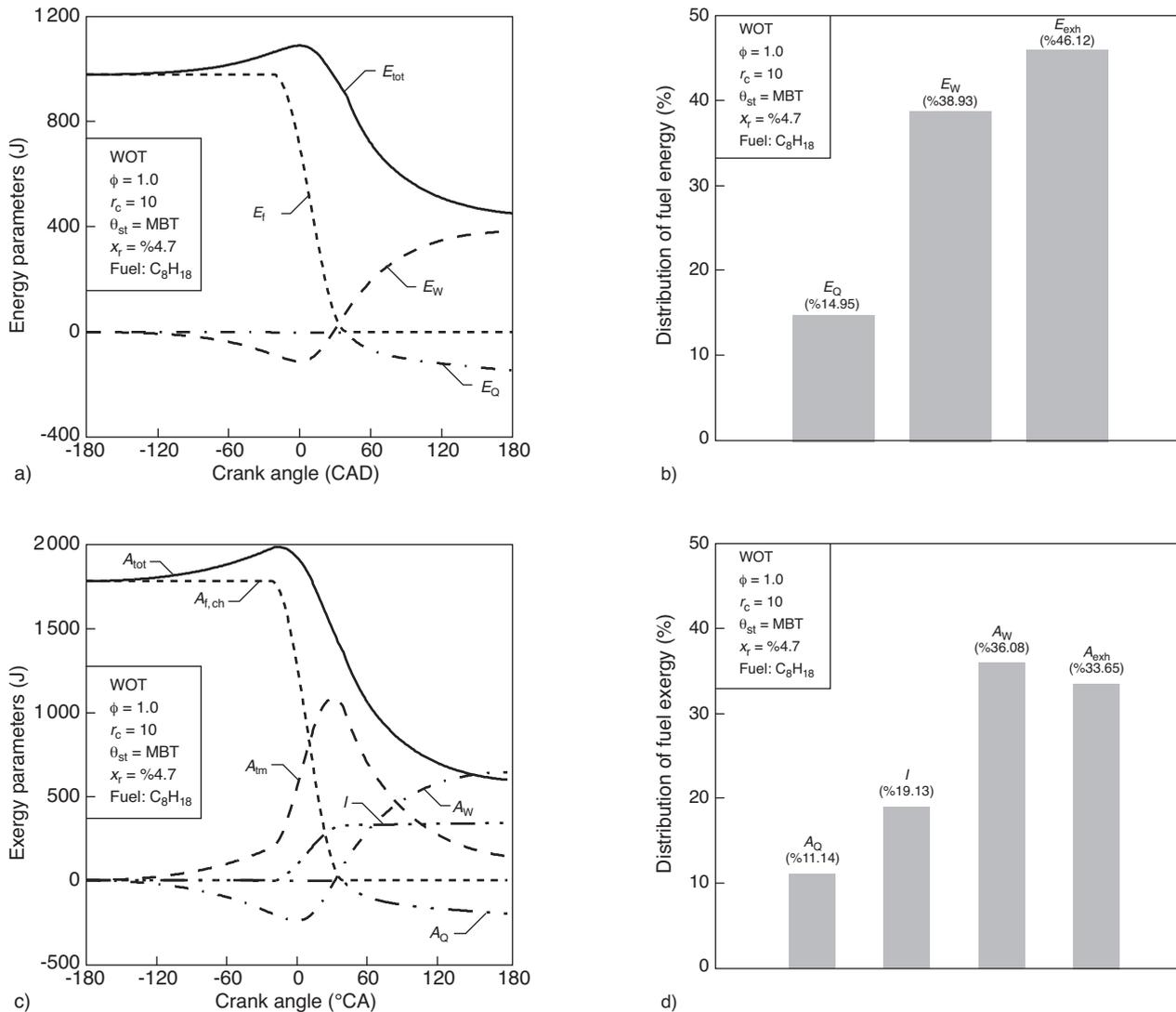


Figure 2

Variation and distribution of energy and exergy parameters.

associated with the cycle duration. The amount of heat transfer to the cylinder wall and consequently  $A_Q$ , is enhanced because of the expanded heat transfer (cycle) duration as the engine speed decreases. Therefore, the higher combustion temperatures occur, as seen in Table 2 because of the decreasing heat transfer since engine speed increases. The extended combustion duration given in Table 2 with increasing engine speed has an additional effect on these higher combustion temperatures. The values of  $A_Q$  for 3 000 rpm and 4 500 rpm are less in magnitude, about 44.9% and 68.4%, than that of 1 500 rpm. The physical meaning of these variations is that low engine speeds give the extra energy loss via increasing heat transfer, while high engine speeds generate the excessive heat loads on engine components because of the high temperatures.

Therefore, medium engine speeds can be evaluated as an ideal operating condition. Exergy transfer with work ( $A_W$ ) in Figure 3b has the maximum values for 3 000 rpm during expansion, while 4 500 rpm gives the highest values during compression because of the advanced spark timing. The negative values of  $A_W$  during compression illustrate that exergy is transferred to the cylinder content from the piston, which corresponds to the compression work. Conversely, exergy is transferred to the piston from the cylinder content during expansion and thus, useful work is obtained. The shortened combustion duration of the low engine speed as seen in Table 2 decreases the useful work by causing an early reduction in the pressure on the piston during expansion and the advanced spark timing of the high engine

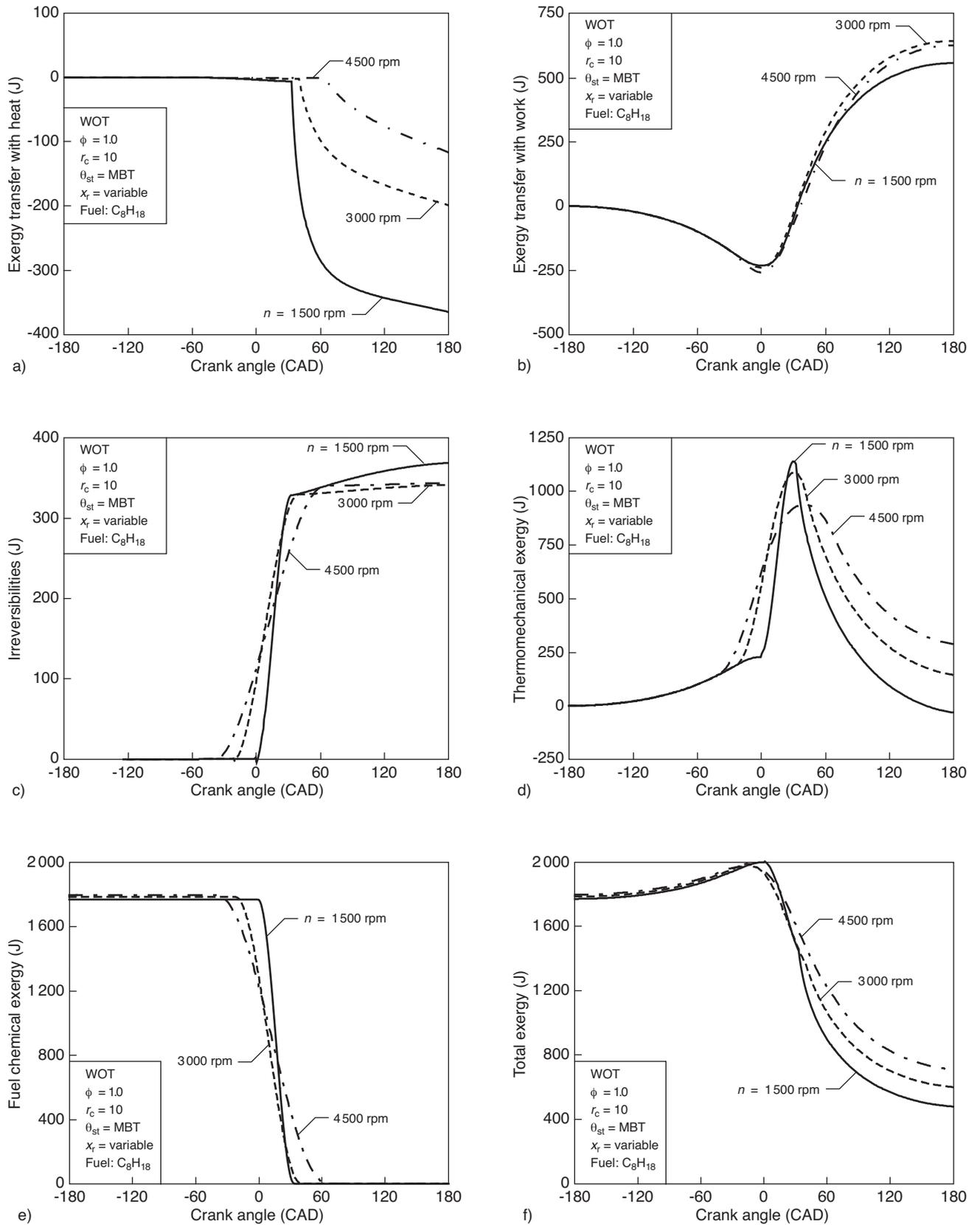


Figure 3  
Variation of exergetic terms with engine speed.

TABLE 2  
The computed cycle and exergetic parameters

Parameters		$m_f$ (g)	$A_{f, ch}$ (J)	$T_{max}$ (K)	$BMEP$ (bar)	$\Delta\theta_b$ (CAD)
$n$ (rpm) @ WOT	1 500	$3.65 \times 10^{-2}$	1 770	2 634	10.1	36
	3 000	$3.68 \times 10^{-2}$	1 784	2 711	11.4	62
	4 500	$3.71 \times 10^{-2}$	1 796	2 743	10.6	105
$BMEP$ (bar) @ 3 000 rpm	4	$1.65 \times 10^{-2}$	800	2 609	4	62
	7	$2.50 \times 10^{-2}$	1 212	2 696	7	63
	10	$3.37 \times 10^{-2}$	1 634	2 761	10	64

speed also creates more compression (negative) work that negatively affects the work output, while the medium engine speed gives the best useful work transfer. This variation can be related to the  $BMEP$  values given in Table 2, because  $BMEP$  is a main indicator of the work obtained during the cycle. The values of  $A_w$  for both 1 500 and 4 500 rpm are less in magnitude, approximately 13.4% and 2.6%, than that of 3 000 rpm. Engine speed of 3 000 rpm also gives the minimum irreversibilities ( $I$ ) in Figure 3c. The irreversibilities for the engine speed of 1 500 rpm increase because of the excessive heat transfer and, as cited in the literature [36], the low combustion temperature as given in Table 2 generates the increments in irreversibilities. On the other hand, the irreversibilities for 4 500 rpm are also relatively higher than 3 000 rpm because of the extended combustion duration as given in Table 2. Thus, the values of  $I$  for 1 500 and 4 500 rpm are greater in magnitude, by about 8% and 0.6%, than that of 3 000 rpm. The variations in  $A_Q$ ,  $A_w$  and  $I$  demonstrate that the engine speed of 3 000 rpm is the optimum speed among the tested engine speeds. Although the inducted fuel mass (or the supplied fuel exergy) is almost unchanged for all engine speeds, as seen in Table 2, the work output of the engine increases thanks to limited irreversibilities for an engine speed of 3 000 rpm. Additionally, 3 000 rpm has reasonable exergy losses with heat interaction. These make 3 000 rpm the best performer in terms of exergy transfer with work output. The variation of thermomechanical exergy ( $A_{tm}$ ) is presented in Figure 3d. The maximum value of  $A_{tm}$  increases and a narrower curve appears as engine speed decreases because of the shortened combustion duration, as seen in Table 2. The variations in  $A_{tm}$  are a combination of the variations in  $A_Q$ ,  $A_w$  and  $I$ . As seen in Figure 3e, fuel chemical exergy ( $A_{f, ch}$ ) does not change significantly with varying engine speed at the start of compression, but the variation in combustion duration shifts the consumption of fuel exergy during combustion. The variations in total exergy ( $A_{tot}$ ) reflect the combination of  $A_{tm}$  and  $A_{f, ch}$  in Figure 3f. The exhaust exergy ( $A_{exh}$ ) that determines the remaining exergy in the cylinder at the end of expansion in Figure 3f increases with increasing engine speed in consequence of expanded combustion duration, which causes higher exhaust temperature and pressure. Thus, more exergy is swept with hotter

exhaust gases as engine speed increases. The values of  $A_{exh}$  are greater in magnitude, by approximately 25.3 and 48% for 3 000 and 4 500 rpm, compared with that of 1 500 rpm.

Figure 4a-f shows the variation of exergetic variables with engine load. Brake Mean Effective Pressure ( $BMEP$ ) is selected to symbolize the engine load, which is varied by adjusting the intake manifold pressure.  $A_Q$  increases with increasing engine load thanks to increasing inducted fuel mass (that means more fuel energy or exergy input), which supplies higher combustion temperatures, as tabulated in Table 2. Therefore, the values of  $A_Q$  are higher in magnitude, by about 69.7% for  $BMEP$  of 7 bar and 169.2% for  $BMEP$  of 10 bar, in comparison with  $BMEP$  of 4 bar. As seen in Figure 4b, exergy transfer with work increases with increasing engine load because of the higher  $BMEP$  values, which are the result of the higher cylinder pressures sourced from the higher fuel energy input, as cited before. Additionally, more compression work is needed as the engine load is increased, as seen in Figure 4b. The increments in  $A_w$  in magnitude are approximately 58.4% for  $BMEP$  of 7 bar and 121.9% for  $BMEP$  of 10 bar compared with  $BMEP$  of 4 bar. Irreversibilities also increase with increasing engine load in Figure 4c. The variation in  $I$  can be attributed to the composition and amount of inducted cylinder charge and combustion products, as cited in the literature. It was declared that the absolute value of the destroyed availability during combustion increases as the inducted fuel mass and combustion-generated products increases [36]. The increments in  $I$  in magnitude are about 46.1% for  $BMEP$  of 7 bar and 97.9% for  $BMEP$  of 10 bar compared with  $BMEP$  of 4 bar. In Figure 4d,  $A_{tm}$  increases with the increasing engine load as a result of variations in exergy transfers with heat and work and also irreversibilities. The variation in  $A_{f, ch}$  is given in Figure 4e; it significantly increases with the increasing engine load. The increment in  $A_{f, ch}$  is sourced from more inducted fuel mass to meet the increasing engine load, as given in Table 2, and also the reduction in the residual gas fraction.  $A_{tot}$  increases naturally with increasing engine load in Figure 4f because the variation in  $A_{tot}$  reflects the combined variations in  $A_{tm}$  and  $A_{f, ch}$ .  $A_{f, ch}$  is dominated during compression, while  $A_{tm}$  is dominated during expansion. In Figure 4f,  $A_{exh}$ , that corresponds

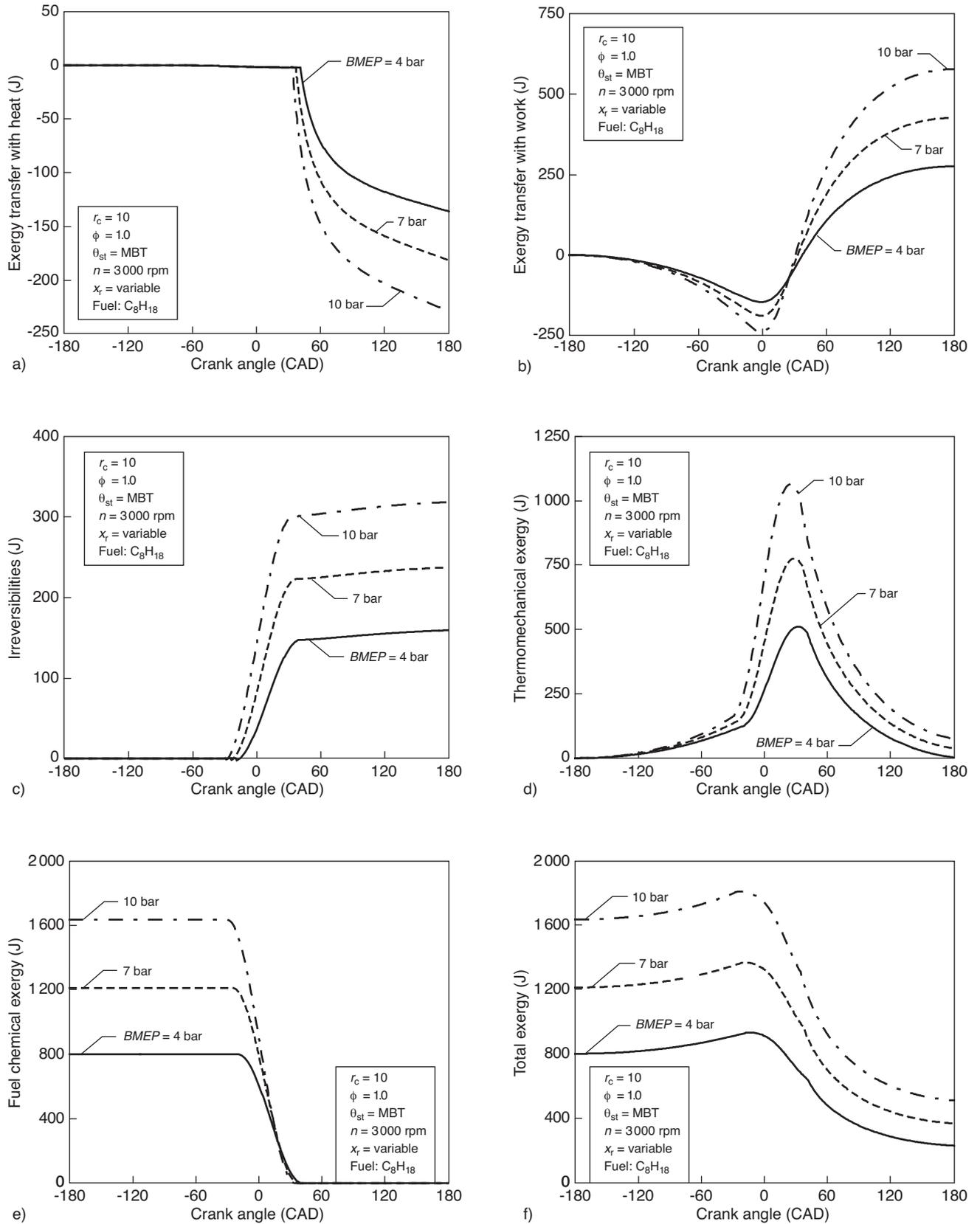


Figure 4  
Variation of exergetic terms with engine load.

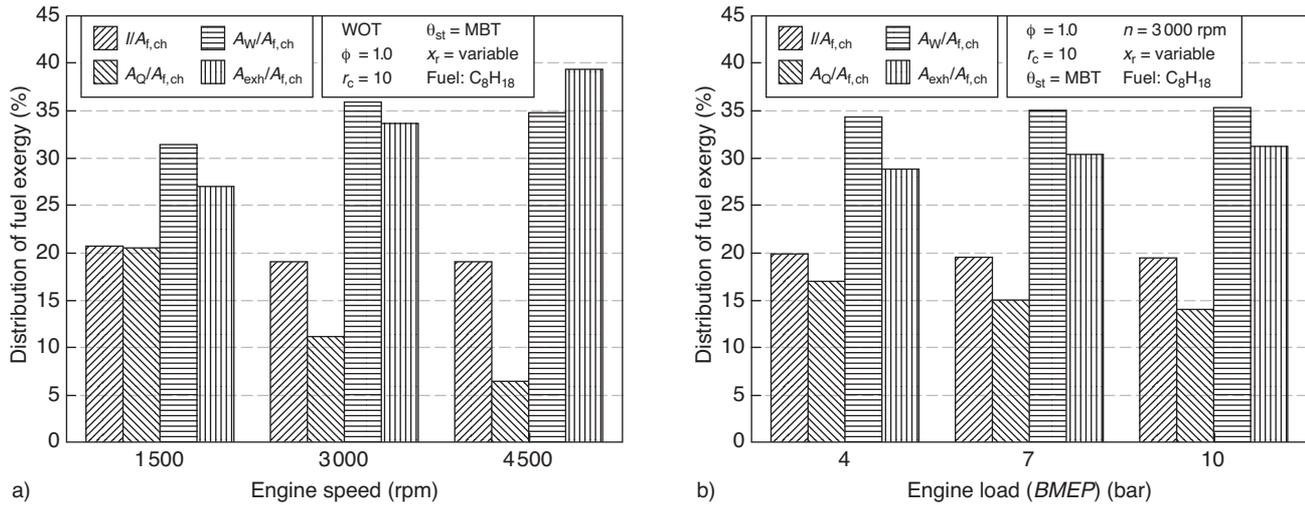


Figure 5

Distribution of fuel exergy for various engine speeds and loads.

to the remaining exergy in the cylinder at the end of the expansion period, also increases with increasing engine load because of more supplied fuel energy to the cylinder, which creates higher cylinder temperatures and pressures. The increments in  $A_{exh}$  in magnitude are about 59.6% for  $BMEP$  of 7 bar and 136.1% for  $BMEP$  of 10 bar when compared with  $BMEP$  of 4 bar.

The distribution of the exergetic variables, *i.e.*  $I$ ,  $A_Q$ ,  $A_W$ ,  $A_{exh}$ , into the fuel exergy (or the normalization of exergetic variables by fuel chemical exergy) for various engine speeds is given in Figure 5a. These data are obtained from the cycle integrated exergy values corresponding to the calculations presented in Figure 3, so generally parallel variations appear in Figure 3 due to the fuel chemical exergy that is almost stable with the varying engine speed. The percentage of  $I$  for 3000 rpm is lower by about 1.7 than 1500 rpm and higher by about 0.01 than 4500 rpm because of the small increase in  $A_{f,ch}$  for 4500 rpm, as seen in Figure 3e, while its magnitude is lower for 3000 rpm. The percentage of  $A_Q$  for 1500 rpm is higher by about 9.5 than 3000 rpm and by 14.1 than 4500 rpm. The percentage of  $A_W$  for 3000 rpm is higher by about 4.5 than 1500 rpm and by 1.1 than 4500 rpm. The percentage of  $A_{exh}$  for 4500 rpm is higher by about 6.7 than 3000 rpm and by 12.4 than 1500 rpm. It can be concluded that the engine speed of 3000 rpm is the optimal speed on the basis of earlier statements related to Figure 3 and the distribution of exergetic variables in Figure 5a due to the fact that it has the ratio of the highest  $A_W$  and acceptable portions of irreversibilities and exergy losses sourced from heat transfer and the exhaust. The distribution of exergetic variables, *i.e.*  $I$ ,  $A_Q$ ,  $A_W$ ,  $A_{exh}$ , into the fuel exergy (or the normalization of exergetic variables by fuel chemical exergy) for various

engine loads is given in Figure 5b. These data are obtained from the cycle integrated exergy values corresponding to the calculations presented in Figure 4, but the variations of some exergetic parameters such as  $I$  and  $A_Q$  are different from the cycle integrated exergy values because of increases in  $A_{f,ch}$ , as seen in Figure 4e. The percentage of  $I$  for  $BMEP$  of 4 bar is higher by about 0.3 than  $BMEP$  of 7 bar and by 0.4 than  $BMEP$  of 10 bar. The percentage of  $A_Q$  for  $BMEP$  of 4 bar is higher by about 2.0 than  $BMEP$  of 7 bar and by 3.0 than  $BMEP$  of 10 bar. The percentage of  $A_W$  for  $BMEP$  of 4 bar is lower by about 0.7 than  $BMEP$  of 7 bar and by 0.9 than  $BMEP$  of 10 bar. The percentage of  $A_{exh}$  for  $BMEP$  of 4 bar is lower by about 1.6 than  $BMEP$  of 7 bar and by 2.4 than  $BMEP$  of 10 bar. It can be concluded that the engine load of 10 bar (high load) is an optimal load in the light of previous statements related to Figure 4 and the distribution of exergetic variables in Figure 5b due to the fact that it has the ratio of the highest  $A_W$  and the lowest portions of irreversibilities and exergy losses except for  $A_{exh}$ .

The variation of the first law efficiency ( $\eta_I$ ), the second law efficiency ( $\eta_{II}$ ) and Brake Specific Fuel Consumption ( $BSFC$ ) for various engine speeds and loads is given in Table 3.  $\eta_I$  and  $\eta_{II}$  are the maximum and  $BSFC$  is the minimum for 3000 rpm, as seen in Table 3. As cited above, the main reason for the best performance of 3000 rpm is that the work output of the engine increases thanks to limited irreversibilities. The less irreversible (or improved) combustion process is also obtained thanks to the increased volumetric efficiency, as given in Table 3. Thus, the engine speed of 3000 rpm gives the best first and second law efficiencies. The second law efficiency also serves as a more realistic evaluation than the first law, because the second law efficiency values for all

TABLE 3  
The performance parameters

Parameters		$\eta_{vol}$ (%)	$\eta_I$ (%)	$\eta_{II}$ (%)	$BSFC$ (g/kWh)
$n$ (rpm) @ WOT	1 500	86.3	33.9	31.5	242.4
	3 000	91.6	38.9	36.1	228.1
	4 500	88.7	37.7	34.9	258.6
$BMEP$ (bar) @ 3 000 rpm	4	41.6	37.1	34.3	293.6
	7	62.5	37.8	35.1	252.1
	10	83.9	38.1	35.3	236.8

engine speeds are lower than those of the first law due to the fact that the chemical exergy of the fuel is higher than its calorific value, as seen in Equations (32, 33). On the other hand, Brake Specific Fuel Consumption is the least for 3000 rpm thanks to the almost stable absolute mass of inducted fuel. The variation in  $\eta_I$ ,  $\eta_{II}$  and  $BSFC$  with respect to the engine load are shown in Table 3.  $\eta_I$  and  $\eta_{II}$  are the maximum and  $BSFC$  is the minimum for  $BMEP$  of 10 bar (high load), as seen in Table 3. The engine work output increases with the increasing engine load due to the increasing inducted fuel mass (which supplies more energy input), as tabulated in Table 2, and the increased volumetric efficiency (which improves the combustion process), as given in Table 3. The decrements in the portion of the irreversibilities and exergy losses except for exhaust exergy thanks to improved combustion make an additional contribution to the first and second law efficiencies and fuel consumption. Thus, the engine load of 10 bar gives the best performance in terms of  $\eta_I$ ,  $\eta_{II}$  and  $BSFC$ .

## CONCLUSIONS

In this study, the effects of some operating parameters such as engine speed and load in Spark Ignition engines are investigated via exergy analysis by using a thermodynamic cycle model. The following conclusions can be drawn from the results of the study:

- exergy transfer with heat decreases, while exergy transfer with exhaust gases increases with the increasing engine speed. Fuel chemical exergy stays almost stable with varying engine speed. A medium engine speed, *i.e.* 3000 rpm, gives the maximum exergy output as work and the minimum irreversibilities. The engine speed of 3000 rpm also gives the best first and second law efficiencies besides the minimum Brake Specific Fuel Consumption. Thus, it can be concluded that medium engine speeds serve both efficient and economical operation in view of exergy analysis;
- exergy transfers with heat, work and exhaust and also irreversibilities increase with the increasing engine load. The fuel chemical exergy also increases as engine load

increases. On the other hand, the percentages of irreversibilities and exergy transfer with heat into the fuel exergy decrease, while the percentage of exergy transfers with work and exhaust increase with increasing engine load. The first and second law efficiencies are the maximum and the Brake Specific Fuel Consumption is the minimum for the high engine load. Thus, it can be concluded that high engine loads serve both efficient and economical operation in view of exergy analysis;

- additionally, it must be noted that engine operation under high engine speeds or high engine load has a wearing and life-consuming effect on engine components because of the friction and thermal load.

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